

Decision Support Principles Applied to Model Mixing

COMPUREG Plzeň, s.r.o.

Nádražní 18 / P.O.Box 334

CZ 306 34 Plzeň

www.compureg.cz

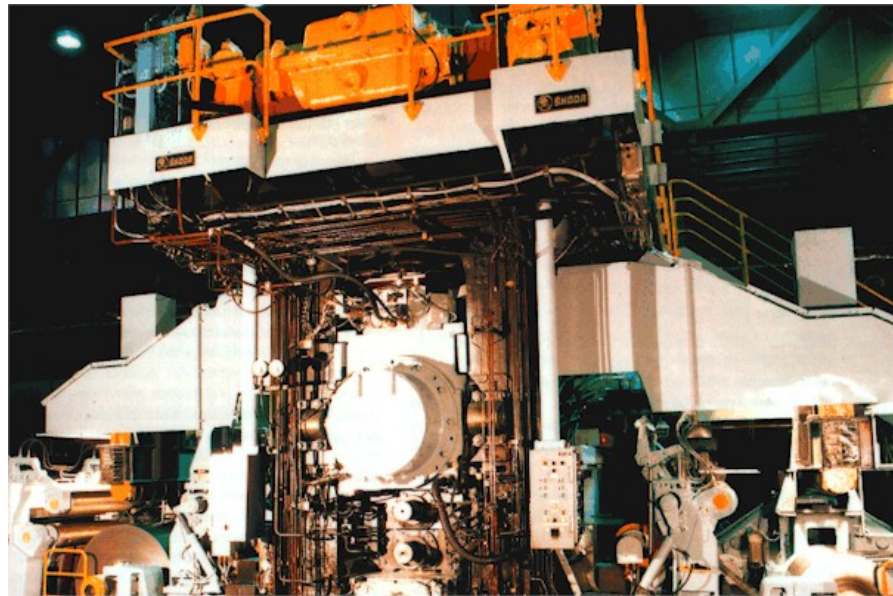
Motivation

- **Decision support methods for industrial applications already elaborated**
- **Complex models may be problematic**
- **Set of cogitable models available**
- **Task: continuous selection of process model (or models)**
- **Possible solution: utilisation of decision support principles**



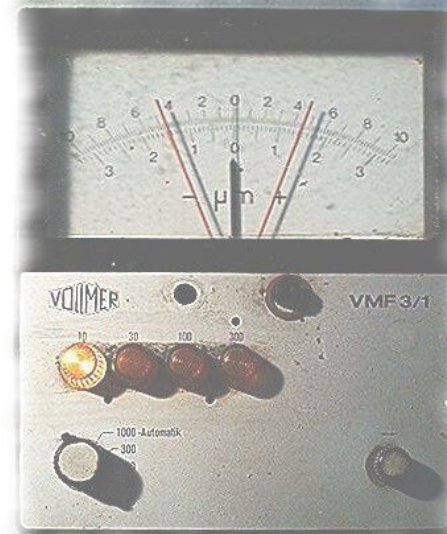
Simple process models

- A process is known to be governed by a physical law \Rightarrow model
- Known stright relations among variables \Rightarrow model
- Several physical laws at once, several relations \Rightarrow a set of models
- Process in question: metall rolling - cold rolling mill



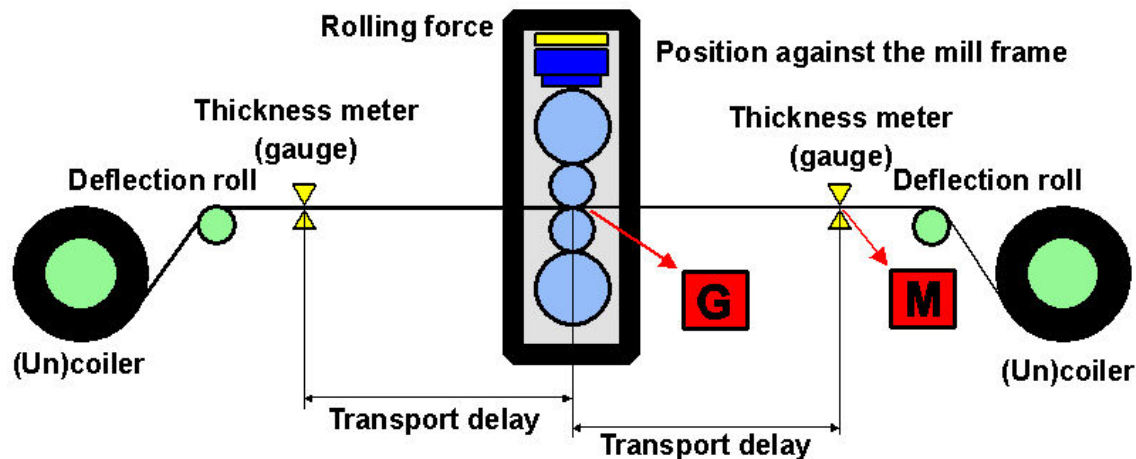
Cold rolling process

- Rolling mill equipped with a control system including AGC
- AGC (thickness control) works excellently under given conditions
- Aim 1: to engage or improve the AGC under adverse conditions
- Aim 2: AGC or operator support for imperfectly equipped rolling mills



Configuration

- **Task: prediction of outgoing thickness in the rolling gap**
- **Significant transport delay inherent for rolling mills**
- **Three or four simple models available**
- **Each model provides a prediction - none of them is perfect**
- **Switching or mixing of models \Rightarrow better prediction ?**



Mixing methods

- **BA - Bayesian averaging**
- **MM - Mixture model**
- **PR - Predictions as regressors**
- **PM - Predictions as regressors in a mixture**

- **Different treatment of uncertainty**
- **Time-delay involved**
- **Case dependent results expected**

BA - Bayesian averaging

- **All unknown quantities interpreted as random variables**
- **Estimation = evaluation of posterior pdf**
- **Pointer to particular model - random variable as well**
- **Estimates interpreted as probabilistic weights evolving according to the Bayes rule**
- **Computational overhead small**

MM - Mixture model

- **BA does not respect the possibility that for some data configuration some model is not updated adequately**
- **Overall predictor interpreted as a mixture of predictors**
- **Probabilistic weights extend the set of unknown parameters**
- **Algorithm called projection-based Bayesian estimation**
- **The weights reflect a degree with which the processed data are in harmony with the updated model**

PR - Predictions as regressors

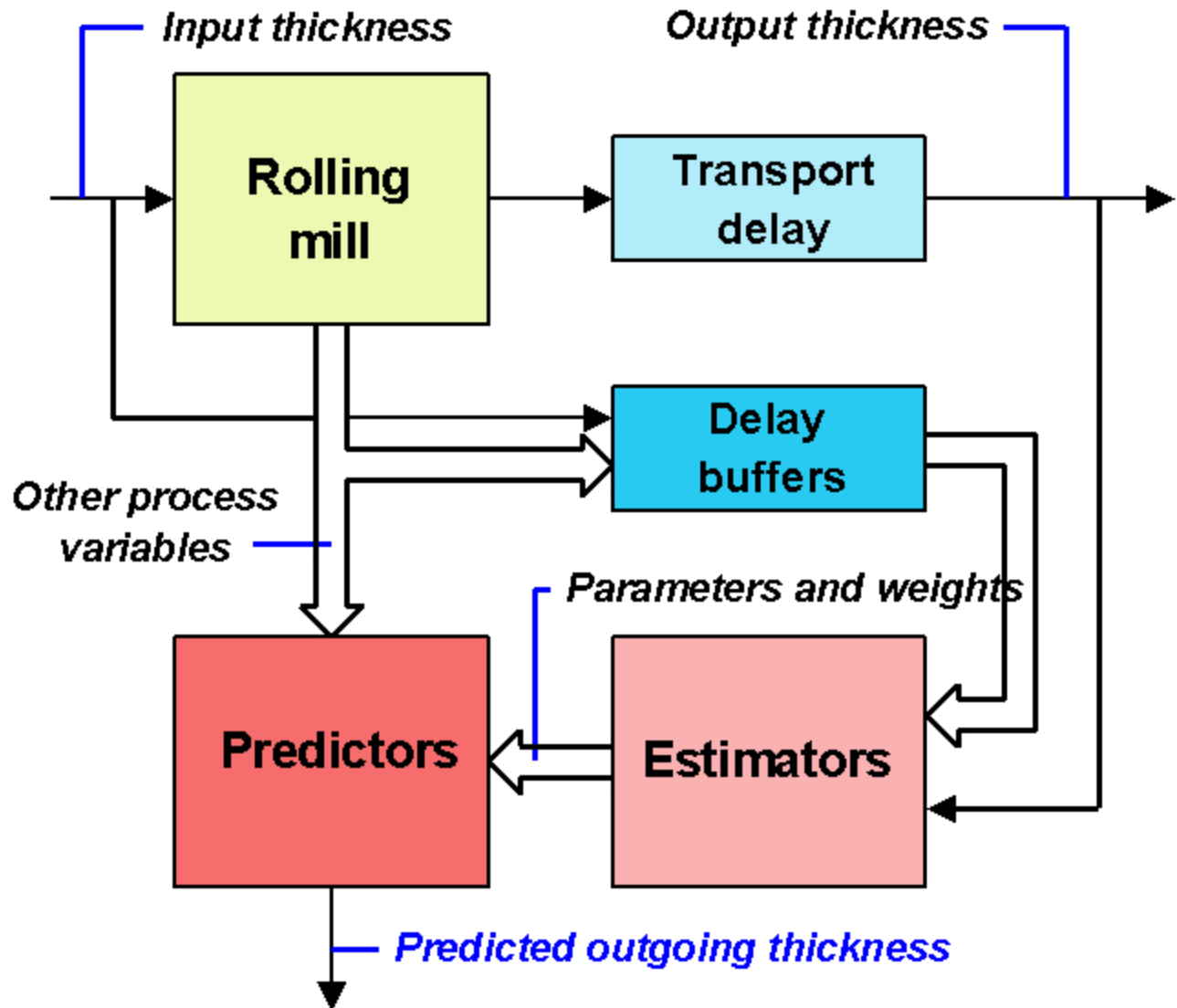
- **BA and MM: overall prediction = convex combination of individual predictions**
- **Problem for cases where the predicted output is outside the “convex hull” of individual model outputs**
- **PR: individual predictions taken as regressors in the overall static model**
- **Estimates $\in \mathbb{R}$, offset estimated as well \Rightarrow overall prediction can be outside the convex hull**
- **Drawback: the same as for BA**

PM - Predictions as regressors in mixture

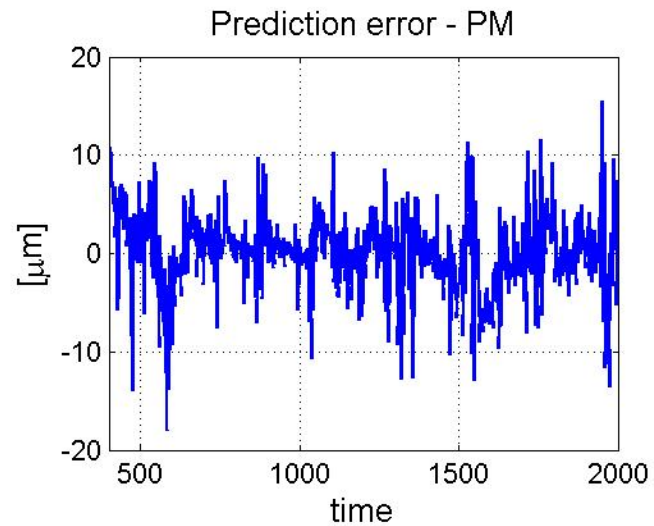
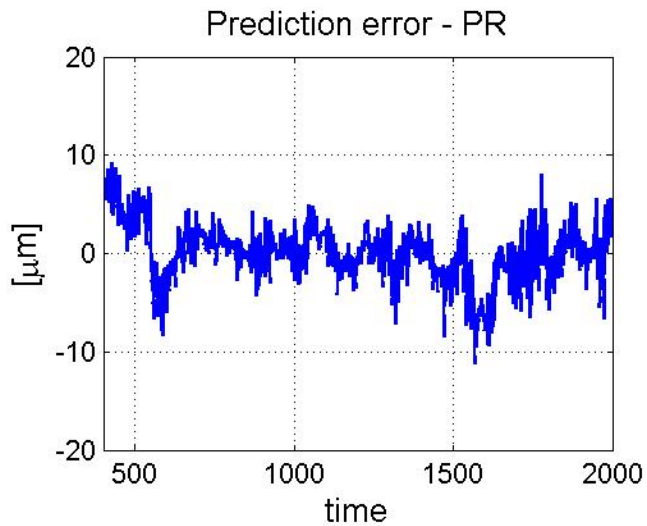
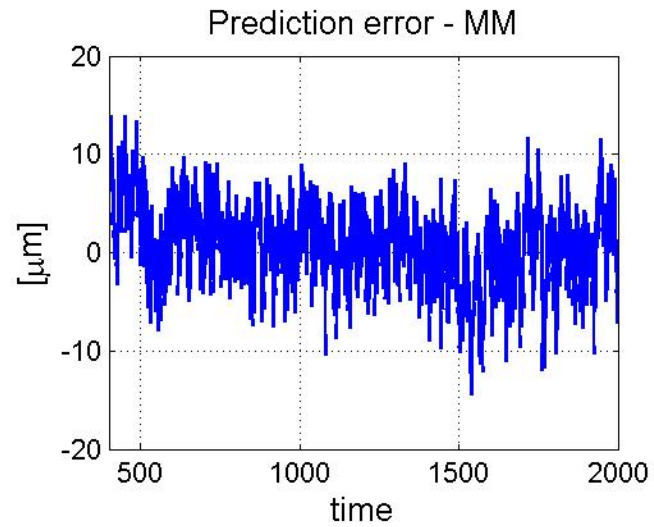
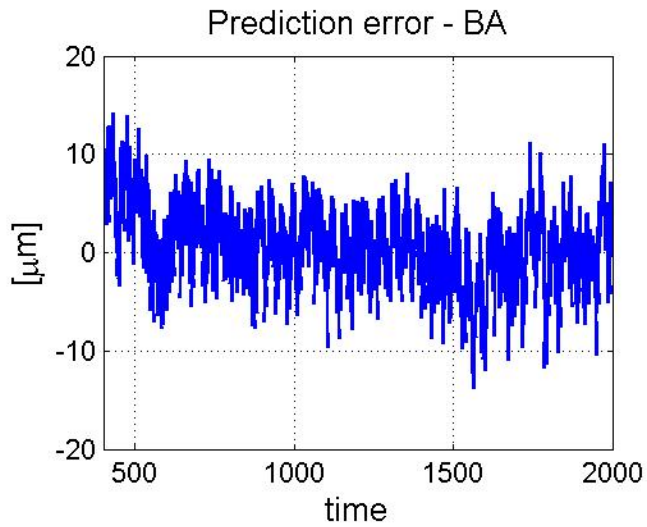
- **Trying to combine advantages of the MM and PR methods**
- **Overall prediction can be “anywhere”**
- **Unequal updating of particular models is respected**



Predictors - schematic diagram

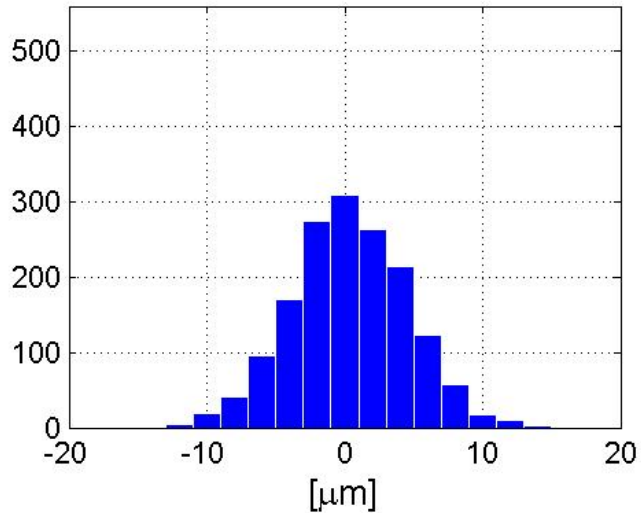


Comparison of results

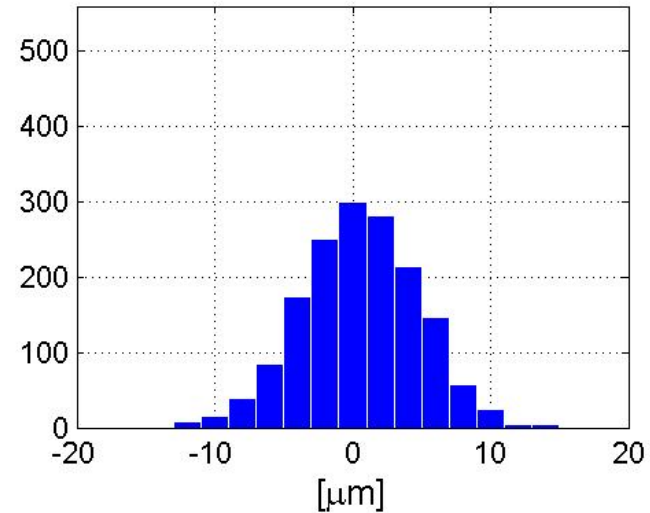


Comparison - histograms

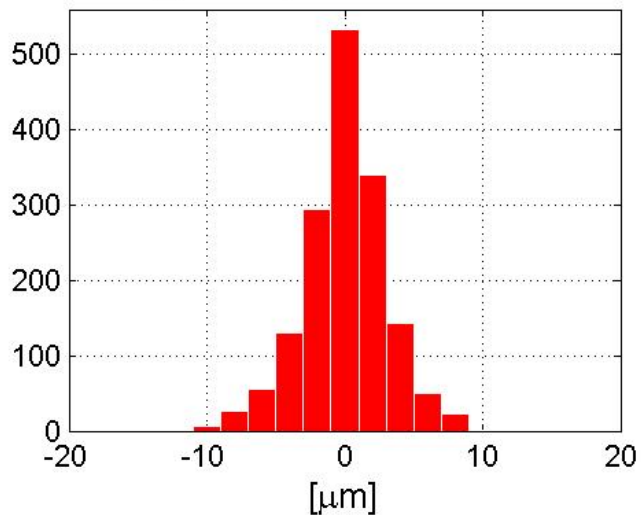
Histogram of prediction error - BA



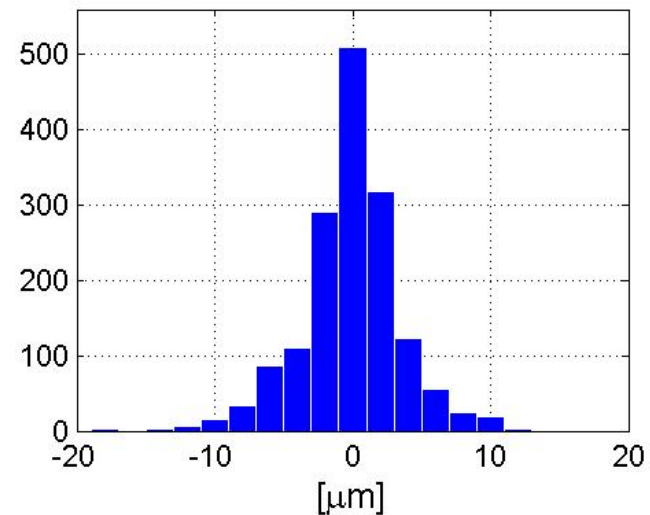
Histogram of prediction error - MM



Histogram of prediction error - PR



Histogram of prediction error - PM



Conclusions

- **Decision support principles were applied for model mixing**
- **Four promising methods introduced**
- **Best results: individual predictions combined into a static regression model (PR)**
- **Results case dependent due to involved approximations**

Publications

Ettler P., Andryšek J.: *Mixing models to improve gauge prediction for cold rolling mills*. IFAC Symposium MMM'07, Quebec City, Canada

Ettler P., Kárný M., Nedoma P: *Model Mixing for Long-Term Extrapolation*. EUROSIM 2007 Congress, Ljubljana, Slovenia