# Dual controller design based on prediction error maximization and partial certainty equivalence

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#### Outline

- Introduction to dual adaptive control
- 2 The goal
- 3 Design of the Dual Controller
  - Formulation of the optimisation problem
  - Solution of the optimisation problem
  - Numerical example
- 4 Conclusion

Conclusion

#### Dual adaptive control

> Control problem with unknown state and parameters

The goal

- > Two conflicting goals meet control objective and improve estimation
- > Aspects of dual control
  - Caution due to inherent uncertainties
  - Probing (Active learning) helps decrease the uncertainty about the unknown state and parameters
- > Optimal adaptive dual control problem mostly cannot be solved analytically

#### Suboptimal solutions

- > with constraint to one-step control horizon
  - Augmenting the cautious control law (Bicriterial controller,...)
  - △ Modification of criterion (e.g. PEDC, IDC, ASOD,...)
- > with two- or multiple step control horizon
  - Criterion approximation (e.g. WDC, Utility cost,...)

#### Requirements of feasible solution

computationally moderate not only for one step ahead horizon

The goal

- ✓ clear interpretation
- ✓ guarantees sufficient control quality

#### Deficiencies of current approaches

teither limited to one step ahead horizon or computationally demanding

#### Steps to fulfil the goal

- formulation of optimisation problem with arbitrary control horizon
- choice of probability density function approximation the would make possible to find closed form solution.
- 3 assurance of both properties of the dual control

#### Goal: to find feasible solution

#### Requirements of feasible solution

- computationally moderate not only for one step ahead horizon
- clear interpretation
- ✓ guarantees sufficient control quality

#### Deficiencies of current approaches

teither limited to one step ahead horizon or computationally demanding

#### Steps to fulfil the goal

- formulation of optimisation problem with arbitrary control horizon
- **2** choice of probability density function approximation the would make possible to find closed form solution.
- 3 assurance of both properties of the dual control

### Considered system

$$s_{k+1} = \mathbf{A}(\boldsymbol{\theta}_k) s_k + \mathbf{B}(\boldsymbol{\theta}_k) \boldsymbol{u}_k + \boldsymbol{w}_k, \tag{1}$$

$$\boldsymbol{\theta}_{k+1} = \boldsymbol{\Phi}_k \boldsymbol{\theta}_k + \boldsymbol{\epsilon}_k, \qquad k = 0, \dots, N-1 \qquad (2)$$

$$\mathbf{y}_k = \mathbf{h}_k(\mathbf{s}_k) + \mathbf{v}_k, \tag{3}$$

 $s_k \in \mathbb{R}^n$  ... non-measurable state  $\theta_k \in \mathbb{R}^p$  ... unknown parameters  $u_k \in \mathbb{R}^r$  ... control  $y_k \in \mathbb{R}^m$  ... measurement

- ✓ The elements of matrices  $A(\theta_k)$  and  $B(\theta_k)$  are known linear function of the unknown parameters  $\theta_k$ .
- ✓ The random quantities  $s_0$ ,  $\theta_0$ ,  $w_k$ ,  $\epsilon_k$  and  $v_k$  are described by known pdf's and are mutually independent.

1/2

### Optimisation problem

### General optimisation problem

The aim is to find control law

$$u_k = u_k(I_k) = u_k(u_0^{k-1}, y_0^k),$$
  $k = 0, 1, ..., N-1$ 

that minimises the following criterion

$$J = E\left\{\mathcal{L}(\boldsymbol{u}_0^{N-1}, \boldsymbol{s}_0^{N-1}, \boldsymbol{\theta}_0^{N-1})\right\}$$

with respect to the system (1)-(3).

Common choice of the cost function  $\mathcal{L}(\boldsymbol{u}_0^{N-1}, \boldsymbol{s}_0^{N-1}, \boldsymbol{\theta}_0^{N-1})$ 

$$\mathcal{L}(\boldsymbol{u}_0^{N-1}, \boldsymbol{s}_0^{N-1}, \boldsymbol{\theta}_0^{N-1}) = \sum_{k=0}^{N-1} (\boldsymbol{s}_{k+1} - \bar{\boldsymbol{s}}_{k+1})^T \boldsymbol{Q}_{k+1} (\boldsymbol{s}_{k+1} - \bar{\boldsymbol{s}}_{k+1}) + \boldsymbol{u}_k^T \boldsymbol{R}_k \boldsymbol{u}_k$$

Conclusion

### Optimisation problem

#### Solvability of the optimisation problem

- general solution given by Bellman optimisation recursion
- analytically unsolvable (due to inherent nonlinearities)
- > it is necessary to use some approximation

$$\rho_k^{CE} = \left\{ p(s_{k+i}, \boldsymbol{\theta}_{k+i} | \boldsymbol{I}_{k+i}) \simeq \delta(s_{k+i} - \hat{\boldsymbol{s}}_{k+i}) \delta(\boldsymbol{\theta}_{k+i} - \hat{\boldsymbol{\theta}}_{k+i|k}); \right\}$$

$$i=0,\ldots,N-k-1$$

$$\rho_k = \left\{ p(\mathbf{s}_{k+i}, \boldsymbol{\theta}_{k+i} | \mathbf{I}_{k+i}) \simeq \delta(\mathbf{s}_{k+i} - \hat{\mathbf{s}}_{k+i}) p(\boldsymbol{\theta}_{k+i} | \mathbf{I}_k); \quad (4) \right\}$$

$$i = 0, \dots, N-k-1$$

Formulation of the optimisation problem

## Optimisation problem

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#### Possible approximation choices

➤ Enforced Certainty equivalence → leads to LQG controller

$$\rho_k^{CE} = \left\{ p(s_{k+i}, \boldsymbol{\theta}_{k+i} | \boldsymbol{I}_{k+i}) \simeq \delta(s_{k+i} - \hat{s}_{k+i}) \delta(\boldsymbol{\theta}_{k+i} - \hat{\boldsymbol{\theta}}_{k+i|k}); \right.$$
$$\left. i = 0, \dots, N-k-1 \right\}$$

➤ Partial Certainty equivalence (PCE)

$$\rho_{k} = \left\{ p(\mathbf{s}_{k+i}, \boldsymbol{\theta}_{k+i} | \boldsymbol{I}_{k+i}) \simeq \delta(\mathbf{s}_{k+i} - \hat{\mathbf{s}}_{k+i}) p(\boldsymbol{\theta}_{k+i} | \boldsymbol{I}_{k}); \right.$$

$$\left. i = 0, \dots, N-k-1 \right\}$$
(4)

#### 1/2

#### Reformulated optimisation problem employing PCE approximation

Control law sought as to minimise the criterion

$$J = E_{\rho_0} \left\{ \mathcal{L}(\boldsymbol{u}_0^{N-1}, s_0^{N-1}, \boldsymbol{\theta}_0^{N-1}) \right\}$$

- $\triangleright$  the expectations determined using  $\rho$  approximation (4)
- > the control law is suboptimal with respect to original formulation
- ➤ not strictly *closed-loop* anymore

#### Adaptive control based on PCE approximation

$$u_{k} = \underset{u_{k}}{\operatorname{argmin}} J_{k} (I_{k}), \qquad k = 0, 1, \dots, N - 1$$

$$J_{k} (I_{k}) = E_{\rho_{k}} \left\{ \mathcal{L}(u_{k}^{N-1}, s_{k}^{N-1}, \boldsymbol{\theta}_{k}^{N-1}) \middle| I_{k} \right\} = E_{\rho_{k}} \left\{ \sum_{i=k}^{N-1} \mathcal{L}_{i} (s_{i}, \boldsymbol{\theta}_{i}, u_{i}) \middle| I_{k} \right\}$$

$$\mathcal{L}_{i} (s_{i}, \boldsymbol{\theta}_{i}, u_{i}) = (s_{i+1} - \bar{s}_{i+1})^{T} \boldsymbol{Q}_{i+1} (s_{i+1} - \bar{s}_{i+1}) + u_{i}^{T} \boldsymbol{R}_{i} u_{i}$$

This controller is of cautious type, i.e. it isn't dual controller!

Conclusion

### Reformulation of the optimisation problem

#### The PCE approximation ensures only cautious behaviour

**?** It is necessary to modify the criterion

#### Useful criterion modification

Cost function used in **Prediction Error Dual Controller (PEDC)**:

$$\mathcal{L}_{i}(\cdot) = (s_{k+1} - \bar{s}_{k+1})^{T} Q_{k+1}(s_{k+1} - \bar{s}_{k+1}) + u_{k}^{T} R_{k} u_{k} - v_{k+1}^{T} \Lambda_{k+1} v_{k+1}$$

- ✓ simple cost function modification with clear interpretation
- ✓ the quality of estimates rated using prediction error
- ✓ the degree of compromise tuned independently for each parameter
- ✓ still analytically solvable using PCE

### Modification of the criterion

#### The modified control objective criterion

$$J_{k} = E_{\rho_{k}} \left\{ \sum_{i=k}^{N-1} (s_{i+1} - \bar{s}_{i+1})^{T} Q_{i+1} (s_{i+1} - \bar{s}_{i+1}) + u_{i}^{T} R_{i} u_{i} - v_{i+1}^{T} \Lambda_{i+1} v_{i+1} \middle| I_{k} \right\}$$

where

$$\mathbf{v}_{i+1} = \mathbf{x}_{i+1} - \hat{\mathbf{x}}_{i+1|i}(\hat{\mathbf{s}}_i, \hat{\boldsymbol{\theta}}_{i|k}), \mathbf{x}_i \triangleq \begin{pmatrix} \mathbf{s}_i \\ \boldsymbol{\theta}_i \end{pmatrix}, \hat{\mathbf{x}}_{i+1|i} \triangleq E_{\rho_k} \left\{ \mathbf{x}_{i+1} \middle| \mathbf{I}_i \right\} = \begin{pmatrix} \hat{\mathbf{s}}_{i+1|i} \\ \hat{\boldsymbol{\theta}}_{i+1|k} \end{pmatrix}$$

and the prediction of the augmented state  $\hat{x}_{i+1|i}$  is defined as

$$\hat{m{x}}_{i+1|i} = \left(egin{array}{cc} m{A}(\hat{m{ heta}}_{i|k}) & m{\mathcal{O}} \ m{\mathcal{O}} & m{\Phi}_i \end{array}
ight) \left(egin{array}{cc} \hat{m{s}}_i \ \hat{m{ heta}}_{i|k} \end{array}
ight) + \left(egin{array}{cc} m{B}(\hat{m{ heta}}_{i|k}) \ m{\mathcal{O}} \end{array}
ight) m{u}_i + \left(egin{array}{cc} \hat{m{w}}_i \ \hat{m{\epsilon}}_i \end{array}
ight).$$

with

$$\hat{\mathbf{s}}_i \stackrel{\Delta}{=} E_{\rho_k} \{ \mathbf{s}_i | \mathbf{I}_i \}, \quad \hat{\boldsymbol{\theta}}_{i|k} \stackrel{\Delta}{=} E_{\rho_k} \{ \boldsymbol{\theta}_i | \mathbf{I}_k \}, \quad \hat{\boldsymbol{w}}_i \stackrel{\Delta}{=} E \{ \boldsymbol{w}_i \}, \quad \hat{\boldsymbol{\epsilon}}_i \stackrel{\Delta}{=} E \{ \boldsymbol{\epsilon}_i \}.$$

### Analysis of the criterion

#### Decomposition of the criterion

$$J_k = J_k^{\mathcal{C}} + J_k^{\mathcal{P}}$$

⇒ it comprises both aspect of the dual control

• Cautious part (it's equivalent to the original quadratic criterion)

$$J_{k}^{C} = \sum_{i=k}^{N-1} (\hat{s}_{i+1|i} - \bar{s}_{i+1})^{T} Q_{i+1} (\hat{s}_{i+1|i} - \bar{s}_{i+1}) + u_{i}^{T} R_{i} u_{i} + E_{\rho_{k}} \left\{ \sum_{i=k}^{N-1} (x_{i+1} - \hat{x}_{i+1|i})^{T} V_{i+1} (x_{i+1} - \hat{x}_{i+1|i}) \middle| I_{k} \right\}$$

Probing part

$$J_{k}^{\mathcal{P}} = -E_{\rho_{k}} \left\{ \sum_{i=k}^{N-1} (x_{i+1} - \hat{x}_{i+1|i})^{T} \mathbf{\Lambda}_{i+1} (x_{i+1} - \hat{x}_{i+1|i}) \left| \mathbf{I}_{k} \right. \right\}$$

### The solution of the modified optimisation problem

#### Bellman optimisation recursion

$$\mathcal{V}_{i}^{o} = \min_{\boldsymbol{u}_{i}} \left\{ \mathcal{V}_{i} \right\} = \min_{\boldsymbol{u}_{i}} \left\{ E_{\rho_{k}} \left\{ \mathcal{L}_{i} + \mathcal{V}_{i+1}^{o} \middle| \boldsymbol{I}_{i} \right\} \right\}, i = N - 1, ..., k, 
\mathcal{V}_{N}^{o} = \boldsymbol{\mathcal{O}},$$

where the cost function at time i denoted  $\mathcal{L}_i$  is defined as follows

$$\mathcal{L}_{i} = (x_{i+1} - \hat{x}_{i+1|i})^{T} (V_{i+1} - \Lambda_{i+1}) (x_{i+1} - \hat{x}_{i+1|i}) + (\hat{s}_{i+1|i} - \bar{s}_{i+1})^{T} Q_{i+1} (\hat{s}_{i+1|i} - \bar{s}_{i+1}) + u_{i}^{T} R_{i} u_{i}.$$

#### Bellman function

$$V_i^o = \hat{\mathbf{s}}_i^T \mathbf{\Pi}_{N-i} \hat{\mathbf{s}}_i + \hat{\mathbf{s}}_i^T \mathbf{F}_{N-i} + \mathbf{F}_{N-i}^T \hat{\mathbf{s}}_i + h_{N-i}, i = N - 1, ..., k,$$
 (5)

from the boundary condition follows that  $\Pi_0$ ,  $F_0$  and  $h_0$  are zero valued

### The dual control law

#### The LQG control law employing certainty equivalence

$$u_{k} = -\left[R_{k} + \boldsymbol{B}^{T}(\hat{\boldsymbol{\theta}}_{k|k})\left(\boldsymbol{Q}_{k+1} + \boldsymbol{\Pi}_{N-k-1}\right)\boldsymbol{B}(\hat{\boldsymbol{\theta}}_{k|k})\right]^{-1} \times \\ \times \left[\boldsymbol{B}^{T}(\hat{\boldsymbol{\theta}}_{k|k})\left(\boldsymbol{Q}_{k+1} + \boldsymbol{\Pi}_{N-k-1}\right)\boldsymbol{A}(\hat{\boldsymbol{\theta}}_{k|k})\hat{\boldsymbol{s}}_{k} + \\ + \boldsymbol{B}^{T}(\hat{\boldsymbol{\theta}}_{k|k})\left(\boldsymbol{Q}_{k+1} + \boldsymbol{\Pi}_{N-k-1}\right)\hat{\boldsymbol{w}}_{k} - \boldsymbol{B}^{T}(\hat{\boldsymbol{\theta}}_{k|k})\boldsymbol{Q}_{k+1}\bar{\boldsymbol{s}}_{k+1} + \\ + \boldsymbol{B}^{T}(\hat{\boldsymbol{\theta}}_{k|k})\boldsymbol{F}_{N-k-1}\right]$$

#### Properties of the dual control law

- > The control law is derived using the Bellman optimisation recursion.
- The dual properties manifested through  $P_{i|k}^{AA}$ ,  $P_{i|k}^{BA}$ ,  $P_{i|k}^{BB}$ ,  $P_{i|k}^{A\Theta}$  and  $P_{i|k}^{B\Theta}$  which depend on  $P_{i|k} = \text{cov}_{\rho_k}(x_i|I_k)$  for i = N 1, ..., k.
- $\triangleright$  Only first two moments of pdf's  $p(x_i|y_0^k)$  are necessary.

#### The dual control law

#### The PCE (cautious type) control law

$$u_{k} = -\left[R_{k} + B^{T}(\hat{\theta}_{k|k}) \left(Q_{k+1} + \Pi_{N-k-1}\right) B(\hat{\theta}_{k|k}) + P_{k|k}^{BB}\right]^{-1} \times \\ \times \left[B^{T}(\hat{\theta}_{k|k}) \left(Q_{k+1} + \Pi_{N-k-1}\right) A(\hat{\theta}_{k|k}) \hat{s}_{k} + P_{k|k}^{BA} \hat{s}_{k} + \\ + B^{T}(\hat{\theta}_{k|k}) \left(Q_{k+1} + \Pi_{N-k-1}\right) \hat{w}_{k} - B^{T}(\hat{\theta}_{k|k}) Q_{k+1} \bar{s}_{k+1} + \\ + B^{T}(\hat{\theta}_{k|k}) F_{N-k-1}\right]$$

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- $\triangleright$  Only first two moments of pdf's  $p(x_i|y_0^k)$  are necessary.

#### Considered system

$$s_{k+1} = \begin{pmatrix} 0 & 1 \\ \theta_1 & \theta_2 \end{pmatrix} s_k + \begin{pmatrix} 0 \\ \theta_{3k} \end{pmatrix} u_k + \mathbf{w}_k$$
$$\mathbf{\theta}_{k+1} = \mathbf{\theta}_k$$
$$y_k = (0, 1)s_k + v_k$$

Initial state and the parameters

$$\begin{array}{l} \Rightarrow \ s_0 = (1, \ -0.5)^T \\ \Rightarrow \ \theta_0 = (-2.0427, \ 0.3427, \ 1)^T \end{array}$$

Noise pdf's

$$p(\mathbf{w}_k) = \mathcal{N}\left((0, \ 0)^T, 0.00012\mathbf{I}_2\right)$$
  
$$p(v_k) = \mathcal{N}\left(0, \ 0.001\right)$$

Prior pdf for EKF

$$\Rightarrow p(\mathbf{x}_0) = \mathcal{N}((1, -0.5, -2.0427, 0.3427, 1)^T, 0.2\mathbf{I}_5)$$

### Criteria parameters

#### Criterion of the original optimisation problem

$$J = E\left\{\sum_{k=0}^{N-1} (s_{k+1,2} - 5)^2 + 0.001 \cdot u_k^2\right\},\,$$

#### Modified criterion for dual control derivation

$$J_k = E_{\rho_k} \left\{ \sum_{i=k}^{N-1} (s_{i+1,2} - 5)^2 + 0.001 \cdot u_i^2 - \mathbf{v}_{i+1}^T \mathbf{\Lambda}_{i+1} \mathbf{v}_{i+1} \Big| \mathbf{I}_i \right\}$$

$$\mathbf{\Lambda}_{i+1} = \begin{pmatrix} 0.5 & \mathbf{\Lambda}_{i+1}^{s,\theta} \\ \mathbf{\Lambda}_{i+1}^{s,\theta} & \mathcal{O} \end{pmatrix}$$

$$\mathbf{\Lambda}_{i+1}^{s,\theta} = \begin{pmatrix} ? & ? & ? \\ ? & ? & ? \end{pmatrix}$$

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$$\mathbf{\Lambda}_{i+1}^{s,\theta} = \left(\begin{array}{ccc} 0 & 0 & 0 \\ ? & ? & ? \end{array}\right)$$

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### Comparison to other controllers

### Control quality comparison using the quality measures $\hat{\mathcal{M}}$ and $\hat{\mathbb{C}}$

	$\hat{\mathcal{M}}$	Ĉ
CE	1.477650	8.245854
PCE	0.902443	1.193457
MSPEDC	0.882633	1.138688

measure of meeting the control objective

$$\hat{\mathcal{M}} = \frac{1}{m} \left\{ \sum_{j=1}^{m} \left( \frac{1}{N} \sum_{i=0}^{N-1} (s_{i+1,2} - 5)^2 \right) \right\}$$

average cost of realising the system trajectory

$$\hat{\mathbb{C}} = \frac{1}{m} \left\{ \sum_{j=1}^{m} \left( \sum_{i=0}^{N-1} (s_{i+1,2} - 5)^2 + 0.001 \cdot u_i^2 \right) \right\}$$

### Concluding remarks

#### Resume

- the new dual adaptive controller with multistage control horizon was introduced
- > some aspects of the criterion and control law were discussed

#### Features of the new dual controller

- clear criterion interpretation
  - modified criterion incorporates both aspects of dual control
  - makes it possible to individually tune influence of parameter uncertainty on control
- ✓ closed form solution available
- ✓ higher control quality compared to CE and PCE controllers
- computationally moderate
- ✓ EKF if sufficient for the estimation of unknown state and parameters
- $\checkmark$  quite robust with respect to choice of weighting matrix  $\Lambda_{i+1}$